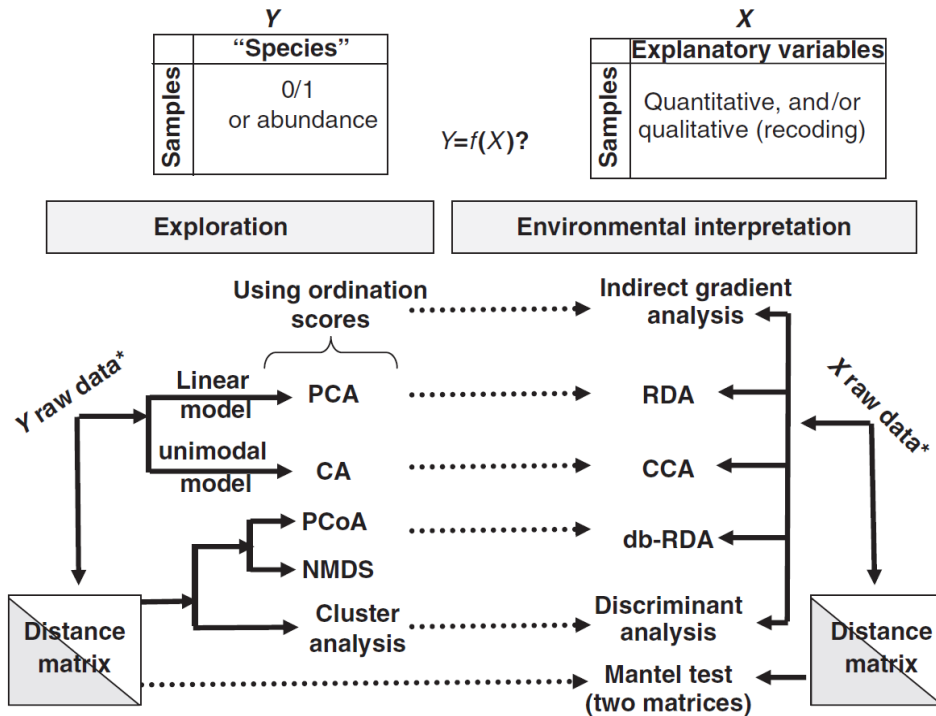


# Auxiliary multivariate analyses

- Linear Discriminant Analysis (LDA)
- Mantel correlation (Mantel correlogram)
- Procrustes rotation and superposition
- ANOSIM (Analysis of Similarity)
- SIMPROF (Similarity Profiles)
- Multivariate permutational ANOVA (PERMANOVA)
- Simper (similarity percentage)
- variance partitioning

...

# Linear Discriminant Analysis (LDA)



Ordination technique maximizing group separation.

LDA uses a **single variable** classifying sites into groups (different to RDA & CCA).

This grouping may represent a hypothesis or be obtained using cluster analysis of **another** dataset.

(important: clustering must have been obtained independently from the variables used in the LDA; otherwise the procedure would be circular)

Note: assumption of homogeneity of within-group covariance (see PERMANOVA)

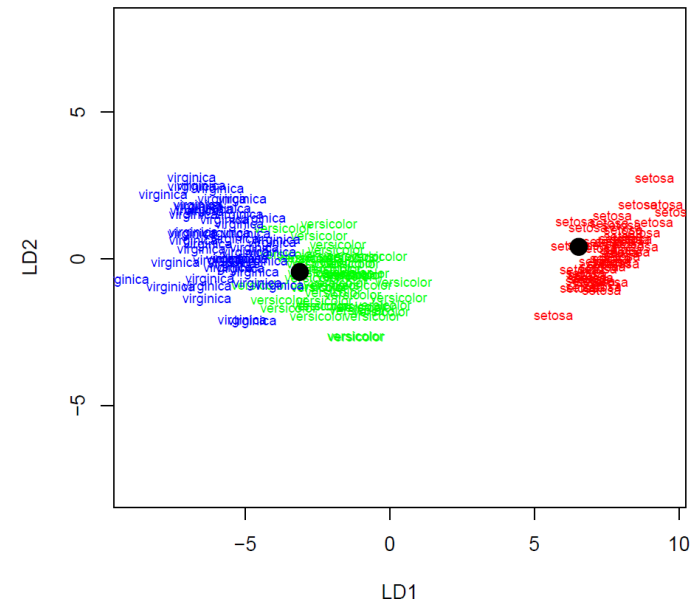
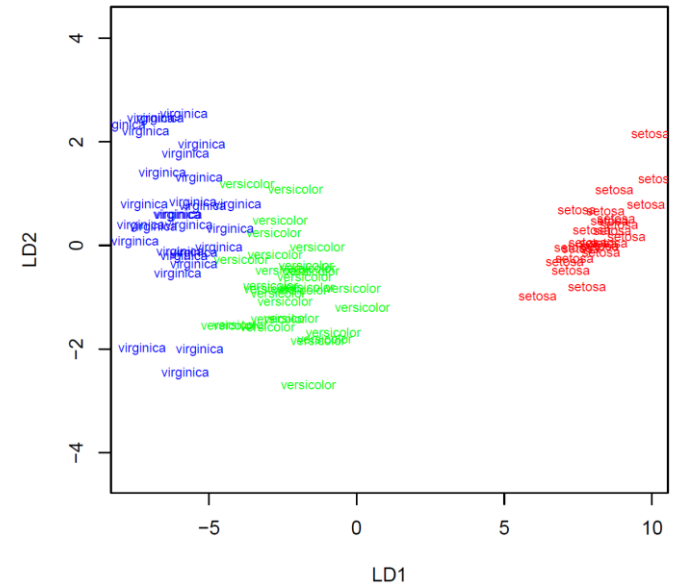
# LDA example: iris dataset

- Iris dataset: measurements of sepal and petal length and width...
- LDA on iris dataset maximizes the separation of the three species

```
>library(mass)
>iris.lda <- lda(Species~., iris)
>plot(iris.lda, col=c("red","green","blue")[iris$Species])
>summary(iris.lda)
```

Can also be used to classify new objects:

```
>predict.unknown.iris<-predict(iris.lda,
newdata=unknown.iris)
>points(predict.unknown.iris$x, pch=16, cex=2)
```



# Mantel test

- test of correlation between two distance or similarity matrices
- Uses permutations to establish significance
- Different types of correlation statistics possible (e.g. Pearson, Spearman, Kendall)
- example:
  - Genetic distance between taxa
  - Environmental dissimilarity or spatial distance
  - Q: is genetic distance between taxa correlated with dissimilarity of the environment, or does genetic distance between taxa increase with increasing spatial distance?

*>mantel(xdis, ydis, method="pearson", permutations=999)*

# Mantel correlogram

example: mite dataset (35 mites at 70 locations, xy coordinates available)

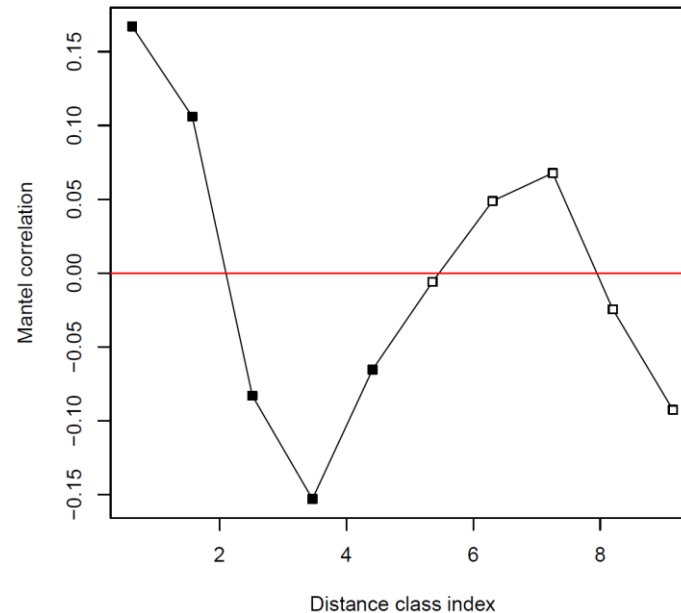
- A correlogram is (typically) a graph in which correlation statistic (i.e. Mantel correlation) is plotted as a function of geographic distance classes (or time lags).

=> test of spatial (or temporal) autocorrelation

- In a Mantel correlogram the correlation is computed between a multivariate distance matrix (e.g. species dissimilarity) and a design matrix (typically spatial/temporal distance classes).

```
>mite.correlog <-mantel.correlog(mite.hel.D, XY=mite.xy,  
n.class=10, r.type="pearson", nperm=999, cutoff=FALSE)
```

	class.index	n.dist	Mantel.cor	Pr(Mantel)	Pr(corrected)
D.cl.1	0.6234366	532.0000000	0.1670561	0.001	0.001 ***
D.cl.2	1.5703098	966.0000000	0.1059971	0.001	0.002 **
D.cl.3	2.5171829	914.0000000	-0.0830506	0.001	0.003 **
D.cl.4	3.4640561	706.0000000	-0.1529721	0.001	0.004 **
D.cl.5	4.4109293	522.0000000	-0.0653801	0.001	0.005 **
D.cl.6	5.3578024	470.0000000	-0.0059279	0.374	0.374
D.cl.7	6.3046756	318.0000000	0.0488553	0.026	0.052 .
D.cl.8	7.2515488	236.0000000	0.0677753	0.008	0.024 *
D.cl.9	8.1984220	120.0000000	-0.0244946	0.217	0.434
D.cl.10	9.1452951	46.0000000	-0.0925184	0.003	0.015 *



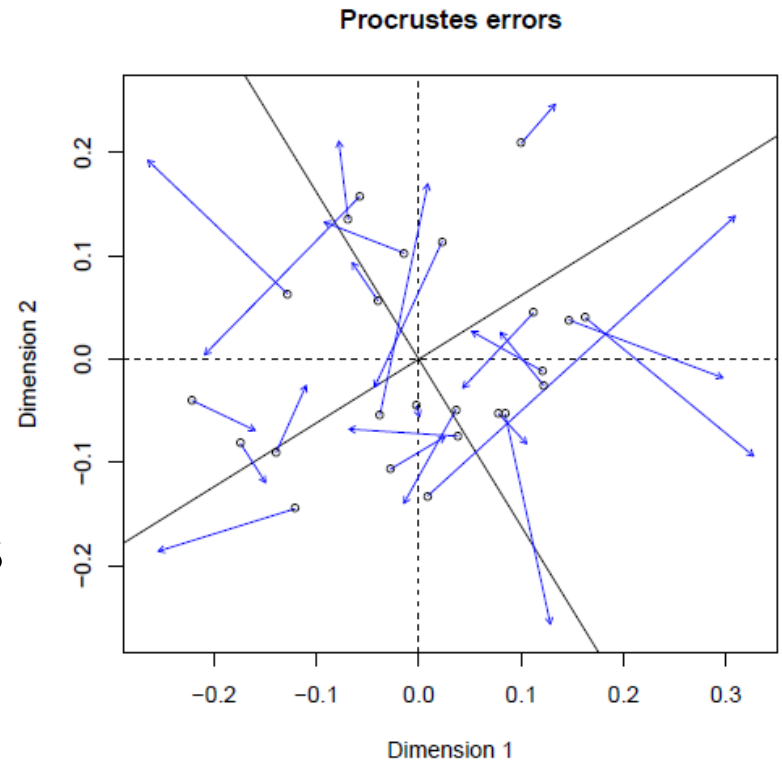
# Procrustes analysis

- *Procrustes rotation* rotates (and rescales) an ordination to maximize similarity with a target ordination.
- Procrustes rotation is typically used for comparison of 2 independent ordinations (superimposition, see example).
- Allows (visual) estimation of the congruence between two ordinations (e.g. two ordinations using different taxa, or two different ordination techniques applied to the same dataset)

>procrustes(X, Y, scale = TRUE)

>protest(X,Y)

See also: co-inertia [ade4::coinertia](#);  
[cocoresp::coca](#)



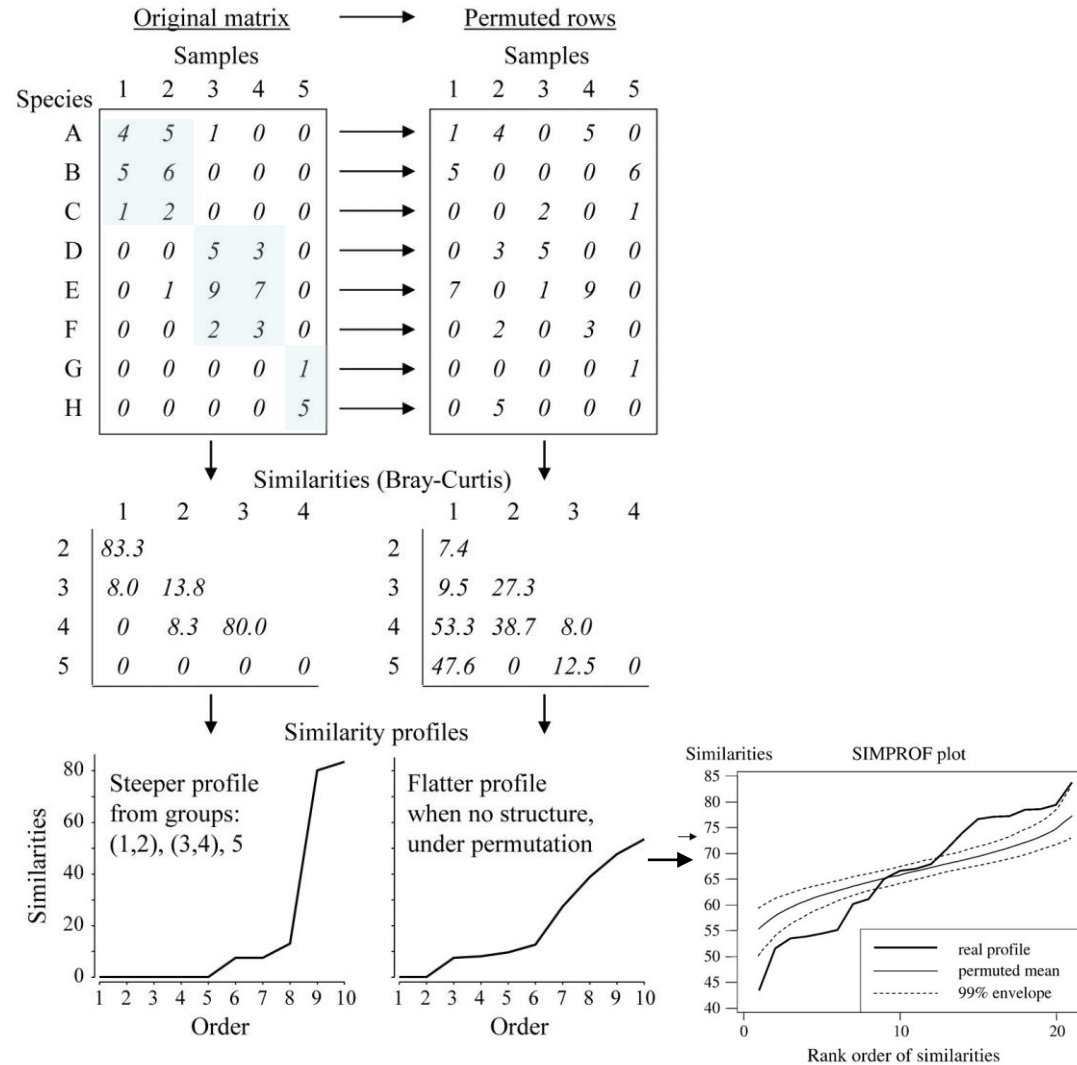
# ANOSIM (Analysis of Similarity)

- A non-parametric (rank) test of difference (equivalent to ANOVA) between groups based on any distance/dissimilarity measure
- significance testing using permutations
- No assumption regarding normality (non-parametric); useful for skewed species abundance data
- example Q: are there differences in similarity between groups of samples?

```
>anosim(species_site_matrix, grouping_sites, permutations =  
999, distance = "bray")
```

# SIMPROF - similarity profile routine

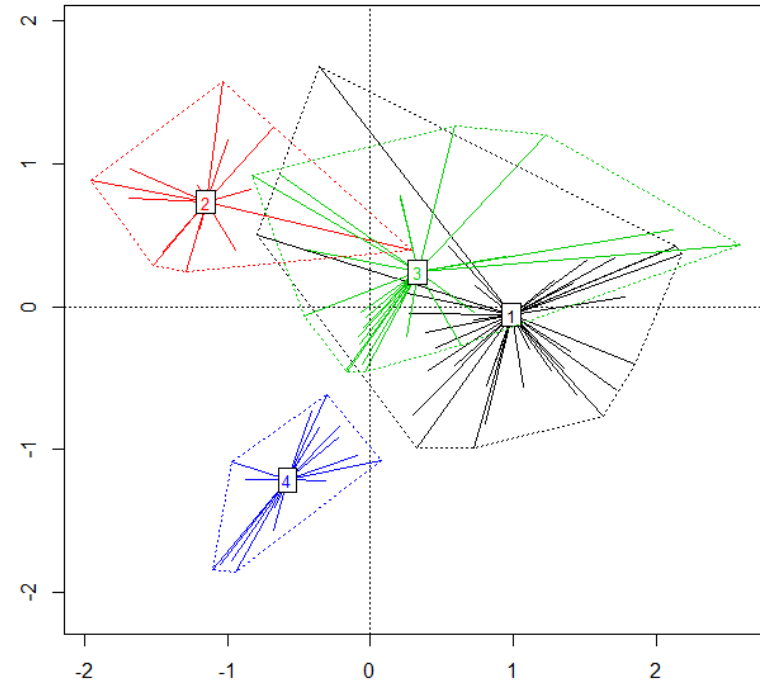
- general test for multivariate structure  
(does not require a priori grouping)
- Q: is there non-random structure in the dataset?
- well-suited in addition to cluster analysis/exploratory analysis



# PERMANOVA/NPMANOVA

- Non-parametric permutation-based test of differences between two or more groups based on any distance measure
- Useful to describing how variation is attributed to different experimental treatments.
- Result depends on **location** and **dispersion**! Location and dispersion effects can be confounded: differences may be caused by different within-group variation (dispersion) instead of different centroids.
- Dispersion (distances of samples from group centroid) is often used for analysis of beta-diversity (*betadisper* in *vegan*).

Note: *betadisper* can be used to check assumption in LDA!



PERMANOVA (test of differences in centroids):  
> `adonis2(dune ~ Management, data=dune.env, permutations=99)`

TEST OF DISPERSION

> `betadisper(d, group, type = c("centroid"), bias.adjust = FALSE)`

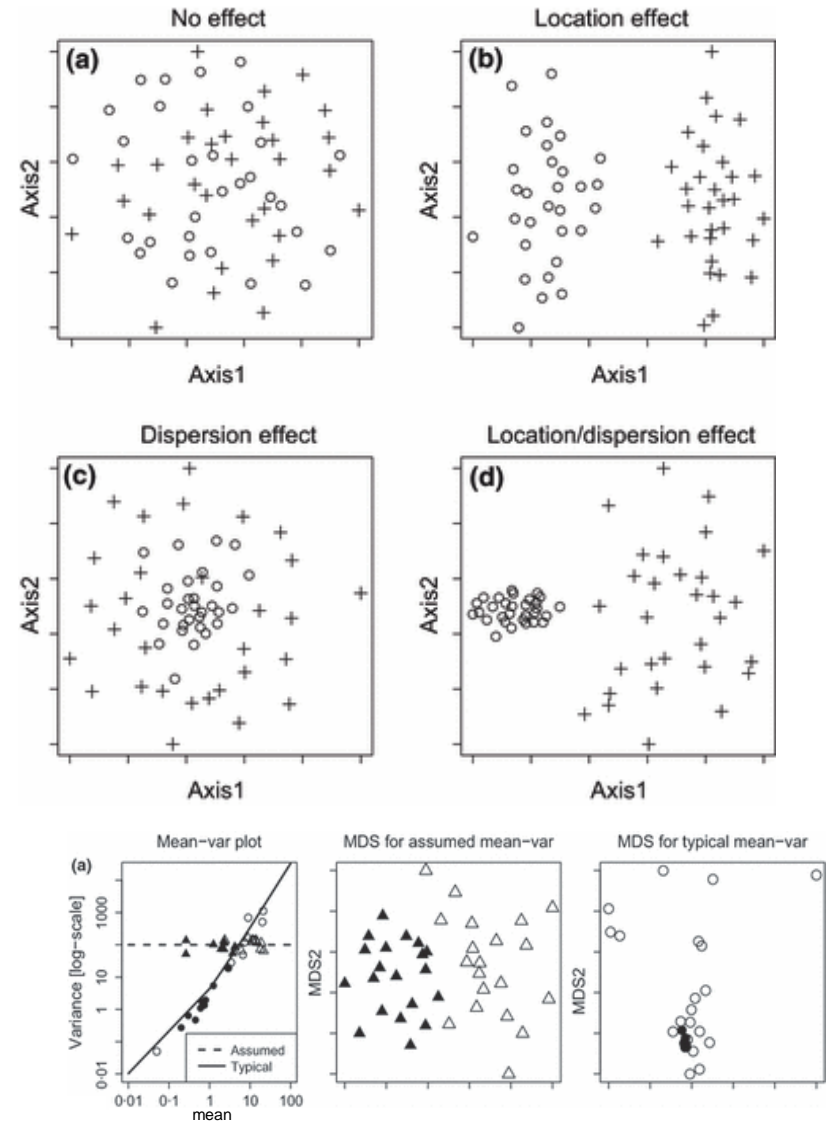
## PERMANOVA, ANOSIM, and the Mantel test in the face of heterogeneous dispersions: What null hypothesis are you testing?

MARTI J. ANDERSON<sup>1,3</sup> AND DANIEL C. I. WALSH<sup>2</sup>

<sup>1</sup>New Zealand Institute for Advanced Study (NZIAS), Massey University, Albany Campus, Private Bag 102 904, Auckland 0745 New Zealand

<sup>2</sup>Institute of Natural and Mathematical Sciences (INMS), Massey University, Albany Campus, Private Bag 102 904, Auckland 0745 New Zealand

- PERMANOVA typically the most powerful and robust technique to test for differences in community structure.
  
- generalised linear models (GLM) can deal with mean-var relationships
  - `R::mvabund`
  - `manyglm(abund~treatment, family="negative.binomial")`



# Simper (similarity percentage)

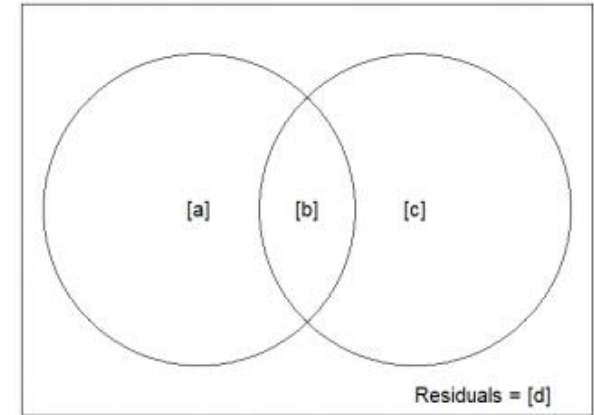
- method for assessing which taxa are primarily responsible for an observed difference between groups of samples.
- typically used with Bray-Curtis similarity.
- example: there are two groups of samples - which taxa contribute to dissimilarity between samples?

```
>simper(comm, group, permutations=999)
```

# Variance partitioning

- Can be used to explain the relative importance (% variance explained) between two or more two sets of explanatory variables (see constrained ordinations).
- Common example: Q: how much variation in a species dataset is explained by the environment compared to spatial distance?
- Results can be visualized using Venn diagram

Venn diagram



```
>browseVignettes("vegan") -> partitioning  
>var_part_results<-varpart(Y,X1,X2, data)  
>showvarparts(var_part_results)
```

[a] - variation explained by dataset X1  
[c] - variation explained by dataset X2  
[b] - shared variation explained by both  
[d] - unexplained variation.

**Note:** for spatial data, consider ordination of the spatial relationships among sampling locations using "spatial eigenvectors (e.g. PCNM, MEM)